

1

$\llbracket [S [NP [N \text{ Ann}]] [VP [V \text{ loves}] [NP [N \text{ Jan}]]] \rrbracket$
 $= \llbracket [VP [V \text{ loves}] [NP [N \text{ Jan}]] \rrbracket (\llbracket [NP [N \text{ Ann}]] \rrbracket)$ S1
 $= \llbracket [VP [V \text{ loves}] [NP [N \text{ Jan}]] \rrbracket (\llbracket [N \text{ Ann}] \rrbracket)$ S2
 $= \llbracket [VP [V \text{ loves}] [NP [N \text{ Jan}]] \rrbracket (\llbracket \text{Ann} \rrbracket)$ S4
 $= \llbracket [V \text{ loves}] \rrbracket (\llbracket [NP [N \text{ Jan}]] \rrbracket) (\llbracket \text{Ann} \rrbracket)$ S6
 $= \llbracket [V \text{ loves}] \rrbracket (\llbracket \text{Jan} \rrbracket) (\llbracket \text{Ann} \rrbracket)$
S6,2,4
 $= \llbracket \text{loves} \rrbracket (\llbracket \text{Jan} \rrbracket) (\llbracket \text{Ann} \rrbracket)$ S5
 $= [\lambda x \ D_e . [\lambda y \ D_e . y \text{ loves } x]](\text{Jan})(\text{Ann})$
 $= [\lambda y \ D_e . y \text{ loves Jan}](\text{Ann})$
 $= \text{Ann loves Jan}$
The sentence „Ann loves Jan“ is true iff Ann loves Jan.

2

- (3) TN: If α is a terminal node, $\llbracket \alpha \rrbracket$ is specified in the lexicon.
(4) NN: If α is a non-branching node and β its daughter, $\llbracket \alpha \rrbracket = \llbracket \beta \rrbracket$.
(5) FA: If α is a branching node, $\{\beta, \gamma\}$ the set of its daughters and $\llbracket \beta \rrbracket$ is a function whose domain contains $\llbracket \gamma \rrbracket$, then $\llbracket \alpha \rrbracket = \llbracket \beta \rrbracket (\llbracket \gamma \rrbracket)$.

3 iff (i) $\llbracket \gamma \rrbracket$ is in the domain of the function $\llbracket \beta \rrbracket$ and (ii) β and γ are in the domain of $\llbracket \rrbracket$.

4 $\llbracket \alpha \rrbracket = \llbracket \beta \rrbracket (\llbracket \gamma \rrbracket)$ if β is a function and γ within its domain, $\llbracket \alpha \rrbracket = \llbracket \gamma \rrbracket (\llbracket \beta \rrbracket)$, if γ is a function and β within its domain

5

$\llbracket [S [NP [N \text{ Ann}]] [VP [V \text{ loves}] [NP [N \text{ Jan}]]] \rrbracket$
 $= \llbracket [VP [V \text{ loves}] [NP [N \text{ Jan}]] \rrbracket (\llbracket [NP [N \text{ Ann}]] \rrbracket)$ FA
 $= \llbracket \text{loves} \rrbracket (\llbracket \text{Jan} \rrbracket) (\llbracket \text{Ann} \rrbracket)$ NNx5
 $= [\lambda x \ D_e . [\lambda y \ D_e . y \text{ loves } x]](\text{Jan})(\text{Ann})$ TN
 $= [\lambda y \ D_e . y \text{ loves Jan}](\text{Ann})$
 $= \text{Ann loves Jan}$
The sentence „Ann loves Jan“ is true iff Ann loves Jan.

6 The main difference between type-driven interpretation and syntax-driven interpretation is, that type-driven interpretation uses general rules independent of what the mother node is (NP, VP, S and so on), and syntax-driven interpretation uses special rules for each mother node. Hence rules S2-5 can be rule 4 (NN) and rules S1 and S6 are rule 5 (FA). Also the rules of syntax-driven interpretation are commutative, while the rules of type-driven interpretation aren't. The merit of using type-driven interpretation rules is, that a single rule for every „type“ of mother node is no longer necessary.

7

A $\llbracket \text{of} \rrbracket = \lambda x \ D_e . x$ B $\llbracket \text{is} \rrbracket = \lambda f \ D_{\langle e, t \rangle} . f$ C $\llbracket \text{a} \rrbracket = \lambda f \ D_{\langle e, t \rangle} . f$ D $\llbracket \text{cat} \rrbracket = \lambda x \ D_e . x \text{ is a cat}$ E $\llbracket \text{proud} \rrbracket = \lambda x \ D_e . x \text{ is proud or } \lambda x \ D_e . [\lambda y \ D_e . x \text{ is proud of } y]$ F $\llbracket \text{in} \rrbracket = \lambda x \ D_e . x \text{ is in or } \lambda x \ D_e . [\lambda y \ D_e . y \text{ is in } x]$ G $\llbracket \text{Texas} \rrbracket = \text{Texas}$ H $\llbracket \text{Joe} \rrbracket = \text{Joe}$ I $\llbracket \text{Mary} \rrbracket = \text{Mary}$

8

A

$$\begin{aligned} & \llbracket [S [NP [N \text{Joe}]] [VP [V \text{is}] [NP [D \text{a}] [N \text{cat}]]] \rrbracket \\ &= \llbracket [VP [V \text{is}] [NP [D \text{a}] [N \text{cat}]] \rrbracket \ (\llbracket [NP [N \text{Joe}]] \rrbracket \) && \text{FA} \\ &= \llbracket [V \text{is}] \rrbracket \ (\llbracket [NP [D \text{a}] [N \text{cat}]] \rrbracket \) (\llbracket [NP [N \text{Joe}]] \rrbracket \) && \text{FA} \\ &= \llbracket [V \text{is}] \rrbracket \ (\llbracket [D \text{a}] \rrbracket \ (\llbracket [N \text{cat}] \rrbracket \)) (\llbracket [NP [N \text{Joe}]] \rrbracket \) && \text{FA} \\ &= \llbracket \text{is} \rrbracket \ (\llbracket \text{a} \rrbracket \ (\llbracket \text{cat} \rrbracket \)) (\llbracket \text{Joe} \rrbracket \) && \text{NNx5} \\ &= [\lambda f \ D_{\langle e, t \rangle} . f]([\lambda f \ D_{\langle e, t \rangle} . f]([\lambda x \ D_e . x \text{ is a cat}])(\text{Joe})) && \text{TN} \\ &= [\lambda f \ D_{\langle e, t \rangle} . f]([\lambda x \ D_e . x \text{ is a cat}])(\text{Joe}) \\ &= [\lambda x \ D_e . x \text{ is a cat}](\text{Joe}) \\ &= \text{Joe is a cat} \end{aligned}$$

B

$$\begin{aligned} & \llbracket [S [NP [N \text{Joe}]] [VP [V \text{proud}] [PP [P \text{of}] [NP [N \text{Mary}]]]] \rrbracket \\ &= \llbracket [VP [V \text{proud}] [PP [P \text{of}] [NP [N \text{Mary}]]] \rrbracket \ (\llbracket [NP [N \text{Joe}]] \rrbracket \) && \text{FA} \\ &= \llbracket [V \text{proud}] \rrbracket \ (\llbracket [NP [N \text{Joe}]] \rrbracket \) (\llbracket [PP [P \text{of}] [NP [N \text{Mary}]]] \rrbracket \) && \text{FA} \\ &= \llbracket [V \text{proud}] \rrbracket \ (\llbracket [NP [N \text{Joe}]] \rrbracket \) (\llbracket [P \text{of}] \rrbracket \ (\llbracket [NP [N \text{Mary}]] \rrbracket \)) && \text{FA} \\ &= \llbracket \text{proud} \rrbracket \ (\llbracket \text{Joe} \rrbracket \) (\llbracket \text{of} \rrbracket \ (\llbracket \text{Mary} \rrbracket \)) \\ &\quad \text{NNx6} \\ &= [\lambda x \ D_e . [\lambda y \ D_e . x \text{ is proud of } y]](\text{Joe})([\lambda x \ D_e . x](\text{Mary})) && \text{TN} \\ &= [\lambda y \ D_e . \text{Joe is proud of } y](\text{Joe})([\lambda x \ D_e . x](\text{Mary})) \\ &= \text{Joe is proud of } [\lambda x \ D_e . x](\text{Mary}) \\ &= \text{Joe is proud of Mary} \end{aligned}$$

C

$$\llbracket [S [NP [N \text{Joe}]] [VP [V \text{is}] [PP [P \text{in}] [NP [N \text{Texas}]]]] \rrbracket$$

$$\begin{aligned}
&= \llbracket [\text{VP } [\text{V is}][\text{PP } [\text{P in}][\text{NP } [\text{N Texas}]]]] \rrbracket \ (\llbracket [\text{NP } [\text{N Joe}]] \rrbracket \) && \text{FA} \\
&= \llbracket [\text{V is}] \rrbracket \ (\llbracket [\text{PP } [\text{P in}][\text{NP } [\text{N Texas}]]] \rrbracket \) (\llbracket [\text{NP } [\text{N Joe}]] \rrbracket \) && \text{FA} \\
&= \llbracket [\text{V is}] \rrbracket \ (\llbracket [\text{P in}] \rrbracket \ (\llbracket [\text{NP } [\text{N Texas}]] \rrbracket \)) (\llbracket [\text{NP } [\text{N Joe}]] \rrbracket \) && \text{FA} \\
&= \llbracket [\text{is}] \rrbracket \ (\llbracket [\text{in}] \rrbracket \ (\llbracket [\text{Texas}] \rrbracket \)) (\llbracket [\text{Joe}] \rrbracket \) && \\
&\quad \text{NNx6} && \\
&= [\lambda f \ D_{\langle e, t \rangle} . f](\llbracket [\lambda x \ D_e . [\lambda y \ D_e . y \text{ is in } x]](\text{Texas}) \rrbracket)(\text{Joe}) && \text{TN} \\
&= [\lambda f \ D_{\langle e, t \rangle} . f](\llbracket [\lambda y \ D_e . y \text{ is in Texas}] \rrbracket)(\text{Joe}) \\
&= [\lambda y \ D_e . y \text{ is in Texas}](\text{Joe}) \\
&= \text{Joe is in Texas}
\end{aligned}$$

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$\llbracket [S [NP [N \text{ Kaline}]] [VP [V \text{ is}] [NP [D \text{ a}] [N [N [A \text{ gray}] [N \text{ cat}]] [PP [P \text{ in}] [NP [N \text{ Texas}]]]]]] \rrbracket$
 $= \llbracket [VP [V \text{ is}] [NP [D \text{ a}] [N [N [A \text{ gray}] [N \text{ cat}]] [PP [P \text{ in}] [NP [N \text{ Texas}]]]]] \rrbracket (\llbracket [NP [N \text{ Kaline}]] \rrbracket)$ FA
 $= \llbracket [V \text{ is}] \rrbracket (\llbracket [NP [D \text{ a}] [N [N [A \text{ gray}] [N \text{ cat}]] [PP [P \text{ in}] [NP [N \text{ Texas}]]]] \rrbracket) (\llbracket [NP [N \text{ Kaline}]] \rrbracket)$ FA
 $= \llbracket [V \text{ is}] \rrbracket (\llbracket [D \text{ a}] \rrbracket (\llbracket [N [N [A \text{ gray}] [N \text{ cat}]] [PP [P \text{ in}] [NP [N \text{ Texas}]]]] \rrbracket) (\llbracket [NP [N \text{ Kaline}]] \rrbracket)$ FA
 $= \llbracket [V \text{ is}] \rrbracket (\llbracket [D \text{ a}] \rrbracket (\llbracket [N [A \text{ gray}] [N \text{ cat}]] \rrbracket (\llbracket [PP [P \text{ in}] [NP [N \text{ Texas}]]] \rrbracket) (\llbracket [NP [N \text{ Kaline}]] \rrbracket))$ FA
 $= \llbracket [V \text{ is}] \rrbracket (\llbracket [D \text{ a}] \rrbracket (\llbracket [N [A \text{ gray}] [N \text{ cat}]] \rrbracket (\llbracket [P \text{ in}] \rrbracket (\llbracket [NP [N \text{ Texas}]] \rrbracket) (\llbracket [NP [N \text{ Kaline}]] \rrbracket)))$ FA
 $= \llbracket [V \text{ is}] \rrbracket (\llbracket [D \text{ a}] \rrbracket (\llbracket [\lambda x \in D_e. \llbracket \text{gray} \rrbracket(x) = 1 \text{ and } \llbracket \text{cat} \rrbracket(x) = 1] \rrbracket (\llbracket [P \text{ in}] \rrbracket (\llbracket [NP [N \text{ Texas}]] \rrbracket) (\llbracket [NP [N \text{ Kaline}]] \rrbracket)))$ PM
 $= \llbracket \text{is} \rrbracket (\llbracket \text{a} \rrbracket (\llbracket [\lambda x \in D_e. \llbracket \text{gray} \rrbracket(x) = 1 \text{ and } \llbracket \text{cat} \rrbracket(x) = 1] \rrbracket (\llbracket \text{in} \rrbracket (\llbracket \text{Texas} \rrbracket) (\llbracket \text{Kaline} \rrbracket)))$ NN
 $= [\lambda x \in D_e. x] ([\lambda f \in D_{\langle e, t \rangle}. f] ([\lambda x \in D_e. [\lambda x \in D_e. x \text{ is gray}](x) = 1 \text{ and } [\lambda x \in D_e. x \text{ is a cat}](x) = 1] ([\lambda x \in D_e. [\lambda y \in D_e. y \text{ is in } x]](\text{Texas}))))(\text{Kaline})$ TN
 $= [\lambda x \in D_e. x] ([\lambda f \in D_{\langle e, t \rangle}. f] ([\lambda x \in D_e. [\lambda x \in D_e. x \text{ is gray}](x) = 1 \text{ and } [\lambda x \in D_e. x \text{ is a cat}](x) = 1] ([\lambda y \in D_e. y \text{ is in Texas}]))(\text{Kaline}))$
 $= [\lambda x \in D_e. x] ([\lambda f \in D_{\langle e, t \rangle}. f] ([\lambda x \in D_e. x \text{ is gray} = 1 \text{ and } x \text{ is a cat} = 1] ([\lambda y \in D_e. y \text{ is in Texas}]))(\text{Kaline}))$
 $= [\lambda x \in D_e. x] ([\lambda f \in D_{\langle e, t \rangle}. f] ([\lambda x \in D_e. x \text{ is gray and is a cat}](\lambda y \in D_e. y \text{ is in Texas}]))(\text{Kaline}))$
 $= [\lambda x \in D_e. x] ([\lambda f \in D_{\langle e, t \rangle}. f] ([\lambda y \in D_e. y \text{ is in Texas}] \text{ is gray and is a cat}))(\text{Kaline}))$
 $= [\lambda x \in D_e. x] ([\lambda f \in D_{\langle e, t \rangle}. f] ([\lambda y \in D_e. y \text{ is in Texas and is gray and is a cat}]))(\text{Kaline}))$
 $= [\lambda x \in D_e. x] ([\lambda y \in D_e. y \text{ is in Texas and is gray and is a cat}]))(\text{Kaline}))$
 $= [\lambda y \in D_e. y \text{ is in Texas and is gray and is a cat}](\text{Kaline}))$
 $= \text{Kaline is in Texas and is gray and is a cat}$